# **REVIEW FOR FINAL EXAM**

## ALGEBRA 32

Below are formulas provided:

$$\boldsymbol{P} = \frac{2\pi}{\omega} \qquad \qquad \omega = \frac{2\pi}{p}$$



$$a_{n} = a_{1} + (n-1)d \qquad a_{n} = a_{1}(r)^{n-1} \qquad S_{n} = a_{1}\left(\frac{1-r^{n}}{1-r}\right)$$
$$S_{n} = \frac{n}{2}(a_{1} + a_{n}) \qquad S_{n} = \frac{a_{1}}{(1-r)}$$

## Suggested YouTube Videos for Some Topics

## **Functions:**

Transforming Piecewise functions: <u>https://www.youtube.com/watch?v=zJ9PD-y1IWY</u> – Move past beginning for examples <u>https://www.youtube.com/watch?v=YEvyJAzTNUk</u>

Evaluating from graph using function notation: https://www.youtube.com/watch?v=kzYtx\_AqzjM https://www.youtube.com/watch?v=uaPm3Tpuxbc

# **Polynomials:**

#### Factoring:

https://www.youtube.com/watch?v=GMoqg\_s4Dl4 https://www.youtube.com/watch?v=GMoqg\_s4Dl4 https://www.youtube.com/watch?v=GMoqg\_s4Dl4

Adding and Subtracting Polynomials: https://www.youtube.com/watch?v=DMyhUb1pZT0 https://www.youtube.com/watch?v=ZgFXL6SEUil

#### Multiplying Polynomials:

https://www.youtube.com/watch?v=fGThIRpWEE4 https://www.youtube.com/watch?v=gg6vUnElXqo

Dividing Polynomials (Long and Synthetic): https://www.youtube.com/watch?v=4u8\_AMacu-Y https://www.youtube.com/watch?v=1byR9UEQJN0 https://www.youtube.com/watch?v=3Ee\_huKclEQ

Writing functions from roots, zeroes, x-intercepts: https://www.youtube.com/watch?v=anWIXiCR01Y

Operations with Complex Numbers: https://www.youtube.com/watch?v=SfbjqVyQljk https://www.youtube.com/watch?v=cWn6g8Qqvs4 https://www.youtube.com/watch?v=tvXRaZbljO8

## **Exponentials:**

Simplifying with rational (fractional) exponents: https://www.youtube.com/watch?v=0z-yIFzpunM https://www.youtube.com/watch?v=KGSvigZQKZY Changing between radical and exponential form: https://www.youtube.com/watch?v=jO4wOQQiVZg https://www.youtube.com/watch?v=zIRKO21qEpQ Graphing Exponentials:

https://www.youtube.com/watch?v=6WMZ7J0wwMI

### Sequences and Series:

Arithmetic Sequences and Series: https://www.youtube.com/watch?v=lj\_X9JVSF8k https://www.youtube.com/watch?v=W95f3ugDqXM

Geometric Sequences and Series: https://www.youtube.com/watch?v=rtsk8caxbr4

# Probability:

Probability with and without replacement: https://www.youtube.com/watch?v=uKTjh-6PFjo Has an ad, sorry https://www.youtube.com/watch?v=ShQu-ly3aE4 https://www.youtube.com/watch?v=w34olO5Phb8 Venn diagrams: https://www.youtube.com/watch?v=jAfNg3ylZAI https://www.youtube.com/watch?v=jAfNg3ylZAI Two Way Tables including Conditional Probability: https://www.youtube.com/watch?v=ETgYbFmV0Ws

# Trigonometry:

Evaluating Angles Using the Unit Circle: https://www.youtube.com/watch?v=NO4H4YROdqk Ignore end about inverses and functions we do not cover https://www.youtube.com/watch?v=IQID5GTsqOw Finds some angles we didn't look at - only do angles w/in one rotation of the circle

Converting Radians to Degrees and Vice Versa: https://www.youtube.com/watch?v=9zspW8u6kQM

Finding other trigonometric functions, given one and quadrant:

https://www.youtube.com/watch?v=L2tNxfipfoQ Only need to find sine, cosine and tangent, ignore other three functions

### Calculators will be allowed on questions notated with (\*\*\*)

### **Functions:**

- 1) Use the function:  $f(x) = 2x^4 x^3 + 3x^2 4x + 6$  to solve each of the following:
- b) f(1) =f)  $f\left(\frac{1}{2}\right) =$ a) f(0) =

- c) f(-1) = d) f(2) = g)  $f\left(-\frac{1}{2}\right) =$ h) f(3) =
- 2) Use the graph below to answer the related questions:
  - a) Over what interval(s) is the function increasing?
  - b) Over what interval(s) is the function decreasing?
  - c) Over what interval(s) is the function constant?
  - d) f(-3) = ?
  - e) f(x) = -3 when x = ?
  - f) 2f(1) = ?
  - g) f(4) + 3 = ?
  - h) What is the y-intercept?
  - i) List the zeroes.



- 3) Use the function f(x) below to perform the transformations for each of the rewritten functions: **DO EACH ON A SEPARATE GRAPH**
- a) g(x) = f(x+2)
- b) h(x) = f(x) 1
- c) a(x) = -f(x)
- d) b(x) = f(x+2) 1
- e) c(x) = f(x-1) + 3



#### **Polynomials**

1) Perform the indicated operation using the functions given below:

 $f(x) = x^3 + 2x^2 - 3x + 5$   $g(x) = 2x^4 + 5x^2 - 10$ 

- a) f(x) + g(x)b) f(x) - g(x)c) 2f(x) + g(x)d) f(x) - 3g(x)e)  $f(x) \times g(x)$ f) 2f(x) + 3g(x)
- 2) Factor each of the following:
  - a)  $f(x) = x^3 + x^2 9x 9$ b)  $g(x) = x^4 - 5x^2 + 4$ c)  $h(x) = 2x^2 + x - 10$ d)  $r(x) = x^2 - 16$ e)  $j(x) = x^3 - 4x^2 - x + 4$ f)  $a(x) = 6x^3 + 12x$

3) Perform the indicated operation on the complex numbers, given that  $i = \sqrt{-1}$ .

a) (5-2i) + (3+4i) b) (3-i) - (7+2i) c) (1-8i)(2+i)

4) Perform long or synthetic division on each of the following, write your result as a polynomial in standard form.

- a)  $(x^3 23x + 28) \div (x 4)$ b)  $(x^4 - 3x^3 + 4x^2 - 5x + 10) \div (x + 3)$ c)  $(2x^4 + 13x^3 + 10x^2 - 18x + 35) \div (x + 5)$ d)  $(x^4 - x^3 + 2x^2 - 7x + 5) \div (x - 1)$
- 5) Match the graph to the function.



1. 
$$f(x) = (x - 1)(x + 3)(x + 5)$$
  
2.  $f(x) = x^2(x - 2)$   
3.  $f(x) = -x(x - 4)(x + 4)$   
4.  $f(x) = x(x - 1)^2(x + 1)$ 

6) Write a possible function, in factored form, for the given graph, using the x-intercepts.





c)



d)



#### **Exponential Functions**

1) Simplify each of the following exponential expressions, write answer in RADICAL FORM.

a) 
$$(x^{7/3})(x^{-2/3})$$
  
b)  $(x^{1/2})(x^{3/4})$   
c)  $\frac{(x^{4/3})}{(x^{2/3})}$   
d)  $(x^{5/3}y^{1/3})(x^{-2/3}y^{4/3})$   
e)  $(x^{5/4}y^{-2/3})(x^{1/4}y^{5/3})$   
f)  $(y^{1/3})(y^{4/3})$ 

- 2) Solve for x:
  - a)  $\sqrt[3]{x-5}+2=0$ b)  $\sqrt{2x+7}=5$ c)  $2\sqrt{x-3}-6=4$ d)  $(2x-4)^{1/2}=12$ e)  $(x-5)^{2/3}=4$ f)  $(x-2)^{3/2}=27$
- 3) Given each of the functions, answer the related questions.
  - a)  $A = 1,000(1+.07)^t$ 
    - 1) Is this growth or decay?
    - 2) What is the initial amount?
    - 3) What is the percent change?
    - 4) How much will there be in 5 years?
  - c)  $A = 925(1 .25)^t$ 
    - 1) Is this growth or decay?
    - 2) What is the initial amount?
    - 3) What is the percent change?
    - 4) How much will there be in 11 years?
  - e)  $A = 600e^{0.81t}$ 
    - 1) Is this growth or decay?
    - 2) What is the initial amount?
    - 3) What is the percent change?
    - 4) How much will there be in 15 years?

- b)  $A = 12,000(1 + \frac{.025}{12})^{12t}$ 
  - 1) Is this growth or decay?
  - 2) What is the initial amount?
  - 3) What is the percent change?
  - 4) How many times is the rate compounded?
  - 5) How much will there be in 7 years?
- d)  $A = 1,200e^{-0.0112t}$ 
  - 1) Is this growth or decay?
  - 2) What is the initial amount?
  - 3) What is the percent change?
  - 4) How much will there be in 5 years?
- f)  $A = 1,000e^{0.0058t}$ 
  - 1) Is this growth or decay?
  - 2) What is the initial amount?
  - 3) What is the percent change?
  - 4) How much will there be in 100 years?
- 4) Graph each of the following, create a table of values using Domain {-2, -1, 0, 1, 2}.

a) 
$$f(x) = 2^x$$
  
b)  $f(x) = -2^x$   
c)  $f(x) = 2^x + 1$   
e)  $f(x) = -3^x$   
f)  $f(x) = 3^x - 2$ 

#### **Sequences and Series**

1) Match each of the following.

Add 5 to each consecutive term	Linear (negative slope)
Subtract 5 to each consecutive term	Exponential Growth
Multiply each consecutive term by 5	Linear (positive slope)
Multiply each consecutive term by $^{1}\!/_{5}$	Exponential Decay

2) \*\*\* Write the rule (equation NOT pattern) for each sequence, and find a<sub>8</sub>.

a)	2, 4, 6, 8	b)	2, 4, 8, 16	c)	-5, -1, 3, 7
d)	-24, 12, -6, 3	e)	18, 9, 0, -9	f)	1, 3, 9, 27

3) \*\*\* Given the rule find the 11<sup>th</sup> term.

a)	$a_n = -5n - 4$	b) $a_n = 5 + 2(n-1)$	c)	$a_n = 200(1/2)^{n-1}$
d)	$a_n = 4(2)^{n-1}$	e) $a_n = 2n^2 - 12$	f)	$a_n = 2(-2)^{n-1}$

4) \*\*\* Find the sum:

$$\sum_{n=1}^{5} 2n - 5 \qquad \qquad \sum_{n=1}^{8} 2(2)^{n-1} \qquad \qquad \sum_{i=1}^{11} 3 - 4i$$

$$\sum_{i=1}^{6} 27(1/3)^{i-1} \qquad \qquad \sum_{j=1}^{5} 3j+8 \qquad \qquad \sum_{j=1}^{3} 7+4j$$

5) \*\*\* Write each series using Sigma notation and solve.

a) 2+4+6+...+98 b) -24+(-20)+(-16)+...+32 c) 1+2+4+...+32

# **Probability**

- 1) \*\*\* Use the given Venn diagram of the probability of an accident on I-95 [P(A)] is 70 % and the probability of an accident on the Merritt [P(B)] is 50%, to answer the related questions?
- a) Find  $P(A \cup B)$ :
- b) Find  $P(A \cap B)$ :
- c) Find  $P(A^c)$ :
- d) Find  $P(A \cup B)^c$ :
- e) Explain a d in context of the problem



- \*\*\* In a class of 25 students, 11 study History and 12 study Geography. There are 5 students who study both History and Geography. How many students study History or Geography? (Drawing a Venn diagram my aid you)
- 3) **\*\*\*** In a group of 100 students, it was found that 40 study Math A, 30 study Drama and 54 study neither. How many students study Math A or Drama? (Drawing a Venn diagram my aid you)
- 4) \*\*\* In a class it was found that 64% of the students like apples, 48% like bananas and 9% like neither. How many students like both apples and bananas? (Drawing a Venn diagram my aid you)
- 5) \*\*\* Use the spinners below to answer the related questions. (Put answer in: reduced fraction, percent rounded to hundredth or decimal rounded to thousandth)
  - a) Using the color spinner, what is the probability of the pointer landing on green?
  - b) Using the number spinner, what is the probability of the pointer landing on a prime number (1 is NOT prime)?
  - c) Using the color spinner and number spinner, what is the probability of the pointer landing on red or an even number?
  - d) Using the number spinner, what is the probability of the pointer NOT landing on 8?
  - e) Using the color spinner and number spinner, what is the probability of the pointer landing on green or 6?





- 6) Write a problem that is an example of independence.
- 7) Write a problem that is an example of dependence.
- 8) \*\*\* Use the two-way frequency table to answer the related questions:

0.1	Preferred Program					
Gender	Dance	Sports	Movies	Total		
Women	16	6	8	30		
Men	2	10	8	20		
Total	18	16	16	50		

- a) The probability the individual prefers the movies.
- b) The probability the individual prefers dance and is a man.
- c) The probability the individual prefers sports, given the individual is a woman
- d) The probability the individual is a woman, given the individual prefers movies
- e) The probability the individual is a man
- f) The probability the individual is a woman who prefers dance
- g) The probability The individual prefers movies, given the individual is a man

## **Statistics**

1) Match each of the following histograms and box plots with its shape description (i – iv).



2) \*\*\* Use the double box and whisker below to answer the related questions



- a) What % of Mr. McPic's class scored between 85 and 95?
- b) What is the median score in Mrs. Frizzle's class?
- c) Would the mean be above or below the median in Mr. McPic's class?
- d) Which class looks like it might have an outlier? Explain.
- e) Can it be said Mr. McPic's class fared better than Mrs. Frizzle's? Defend your position.
- f) What is Q1 in Mrs. Frizzle's class? In Mr. McPic's class?

The histogram below shows the ages of individuals entering a local store. The mean age of the individuals is
 37.5 with a standard deviation of 7.5. Answer the related questions below.



Histogram for Age

- a) What is the interval of ages, one standard deviation from the mean?
- b) How many people fall within one standard deviation from the mean?
- c) Mark the mean and one standard deviation from the mean on the chart and shade that area of the histogram.
- 4) \*\*\* The mean of a set of 5 numbers is 26, with a median of 25 and standard deviation of 5, if all of the numbers were increased by 10
  - a) What would the mean be?
  - b) What would the median be?
  - c) What would the standard deviation be?
  - d) What is you changed THE ORIGINAL numbers to %s, by dividing by 100, how would this change the mean, median and standard deviation?
- 5) Determine the population, sample, parameter and its value, statistic and its value, margin of error and statistical range for each of the following.
  - a) According to the world genetics foundation 36.2% of all boys age 5 10 carry the blue eyed gene, a study of

308 random boys age 5 - 10 found 34% of them carried the blue eyed gene.

- i. Population:
- ii. Parameter
- iii. Sample
- iv. Statistic
- v. Margin of Error
- vi. Statistical Interval
- vii. What happens to the margin of error when you reduce the number of your study? Increase the number in your study?

- b) The Connecticut State Employee Human Resources data base shows 11.6% of employees live outside the state, a study of 1200 Connecticut State Employees found that 12% of them lived outside the state.
  - i. Population:
  - ii. Sample
  - iii. Parameter
  - iv. Statistic
  - v. Margin of Error
  - vi. Statistical Interval
  - vii. What happens to the margin of error when you reduce the number of your study? Increase the number in your study?
- 6) Fairfield Woods Middle school did a survey 100 random FWMS students, to find out how many students are driven to and from school (as opposed to riding a school bus or walking). They found that 32% of students are driven to and from school.
  - a) Can the school board use this information for planning the number of busses needed for the entire middle school district (FWMS, TMS, RLMS)? Explain why.
  - b) Can the school board use this information for planning the number of busses needed for Fairfield Woods Middle School? Explain why.

#### **Trigonometry**

- 1) What is 200<sup>°</sup> in radians?
- 2) What is  $\frac{\pi}{18}$  in degrees?
- 3) Find the exact value of each:

a)	sin 150°	b)	cos 240°	c)	tan 135°	d)	$\sin\frac{\pi}{3}$	e)	$\cos\frac{\pi}{4}$
f)	sin 240°	g)	cos 225°	h)	tan 120°	i)	$\sin \frac{3\pi}{4}$	j)	$\tan \frac{\pi}{6}$

4) Use the given value and quadrant to determine the value requested:

- a) Given  $tan\theta = \frac{3}{4}$ and  $180 < \theta < 270$ , find  $sin\theta$ b) Given  $cos\theta = \frac{1}{2}$ and  $0 < \theta < 90$ , find  $sin\theta$ . c) Given  $sin\theta = \frac{1}{2}$ and  $90 < \theta < 180$ , find  $cos\theta$ .
- 5) Graph 1 period of the functions below. Remember to label your scale and axes.
- a) f(x) = sin(x)b) f(x) = cos(x)c) f(x) = 2sin(x)d) f(x) = cos(x) - 1e) f(x) = sin(x) + 2f) f(x) = -cos(x)
  - 6)  $f(x) = 3\cos(2x)$ 
    - a. What is the amplitude?
    - b. What is the period?
    - c. What is the horizontal shift?
    - d. What is the vertical shift?
    - e. Identify any other transformations on the curve.

7) f(x) = -4sin(x) + 2

- a. What is the amplitude?
- b. What is the period?
- c. What is the horizontal shift?
- d. What is the vertical shift?
- e. Identify any other transformations on the curve.

8)  $f(x) = 2\cos(x - 30) - 1$ 

- a. What is the amplitude?
- b. What is the period?
- c. What is the horizontal shift?
- d. What is the vertical shift?
- e. Identify any other transformations on the curve.

9) Convert 330° to radians and draw it in the correct quadrant. What is the reference angle?



Radian measure:
Reference angle:

What quadrant is it in? \_\_\_\_\_

19) Engineers at the Big E are attempting to model the motion of the Ferris wheel. The Ferris wheel has a radius of 24 ft and the rider is 3 ft above the ground at the lowest point. When operating at full speed, the rider makes one counter-clockwise revolution every 2 minutes (120 seconds).

a. Graph one rotations. Label x and y axes with all relevant points AND what each represents.



- b. Use sine to write a function to model the height of the rider starting with t = 0 sec when the rider is at the bottom and reaches the top of the Ferris wheel after a  $\frac{1}{2}$  rotation. Find the value of A and B and explain the meaning of each parameter (A,  $\omega$ , B) of the function as it relates to the Ferris wheel model.
  - a. Function:  $h(t) = Asin(\pi x \pi/6) + B$
  - b. Amplitude:
  - c. Midline:
  - d. Period:
- c. At what time(s) is the car A (assuming it started at the bottom at time zero) at 27 feet above the ground? (Only use first rotation)
- d. How high is car A at 30, 60, and 90 seconds?